

Foundations 12

Chapter 3 - class notes

Set - a group of things

ex. set of whole numbers $W = \{0, 1, 2, 3, \dots\}$

universal set - complete set

ex. Vowels $V = \{A, E, I, O, U, Y\}$

Subset - a set whose elements all belong to another set

ex. Vowels is a subset of all the letters in the alphabet (A)

written like $\Rightarrow V \subset A$ means subset

Complement - all the elements of a universal set that do not belong to a subset.

ex. V' \Rightarrow would be all the consonants except Y.

Empty set - a set with nothing in it

ex. a set of odd number that can be evenly divided into two parts would be an empty set

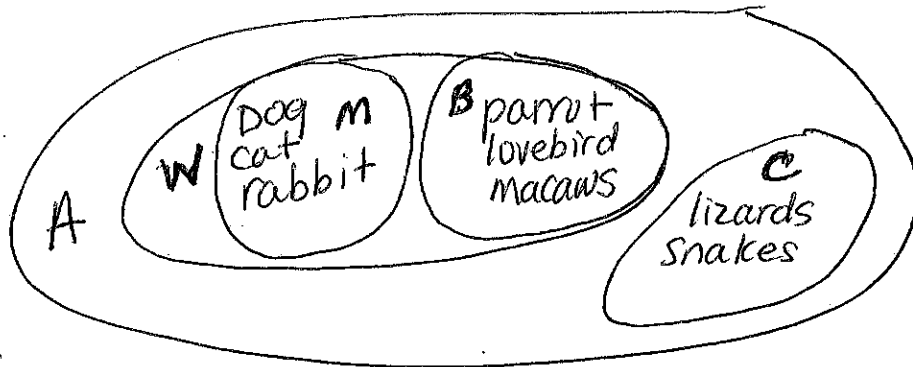
disjoint - 2 ^{or more} sets with nothing in common.

$$O = \{1, 3, 5, 7, 9\} \quad E = \{2, 4, 6, 8\}$$

\downarrow $E = O'$ and they are disjoint sets
 $E' = O$

$N = \text{natural numbers } N = \{1, 2, 3, 4, \dots\}$
 $W = \text{whole numbers } W = \{0, 1, 2, 3, 4, \dots\}$
 $I = \text{integers } I = \{\dots, -2, -1, 0, 1, 2, \dots\}$

ex $A = \text{all animals}$
 $W = \text{warm blooded}$
 $C = \text{cold blooded}$
 $M = \text{mammals}$
 $B = \text{Birds}$



Subsets

$W \subset A$
 $C \subset A$
 $M \subset W$
 $B \subset W$

$W' = C$
 $C' = W$

mutually exclusive: 2 or more events that cannot happen at the same time.

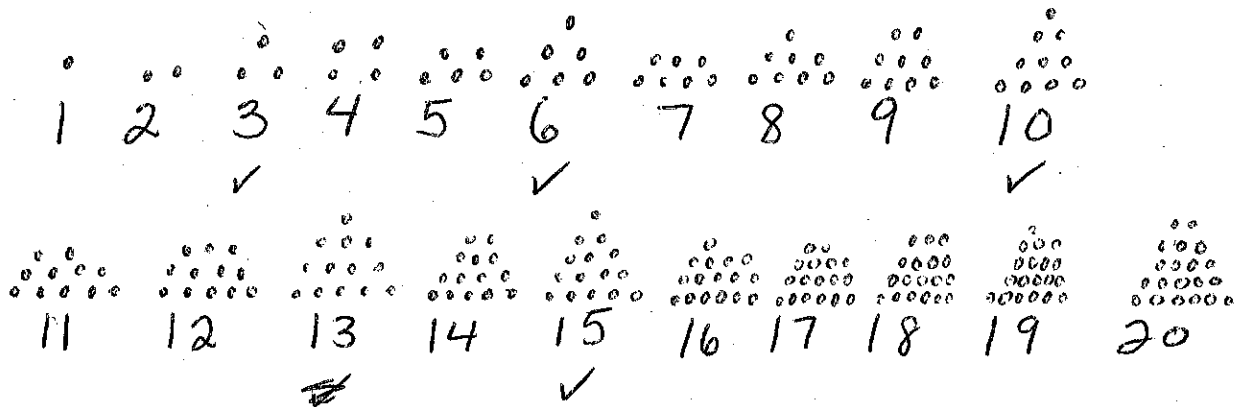
ex 2

$U = \{ \text{natural numbers from 1 to 20} \}$

$T = \{ \text{triangular numbers from 1 to 20} \}$

$E = \{ \text{even triangular numbers from 1 to 20} \}$

$n(\underset{\substack{\uparrow \\ \text{set}}}{\quad}) \Rightarrow \text{number of things in a set}$



$U = \{ 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20 \}$

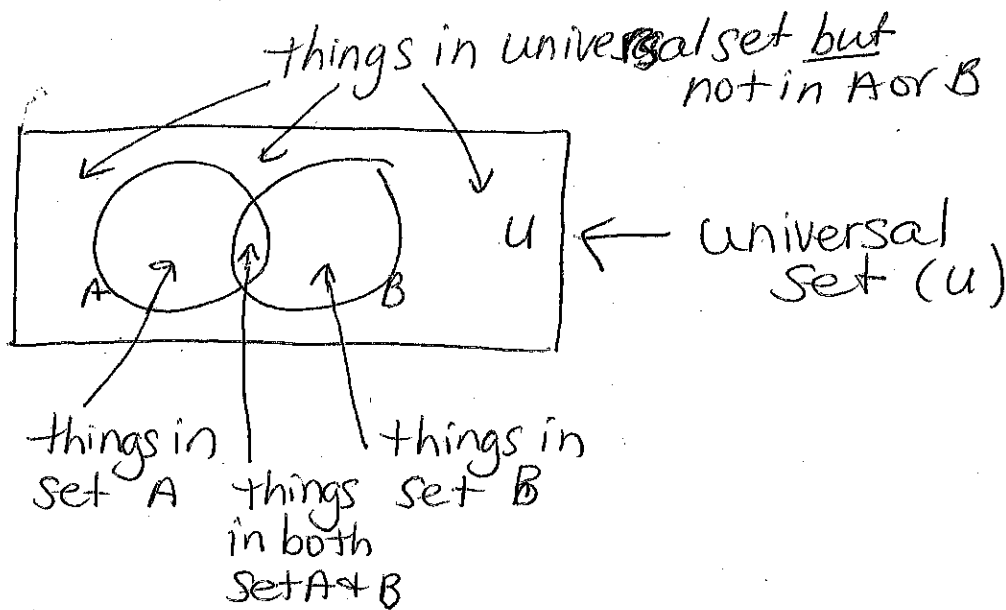
$n(U) = 20$

$T = \{ 3, 6, 10, 15 \}$ $n(T) = 4$

$E = \{ 6, 10 \}$ $n(E) = 2$

$\therefore E \subset T \subset U$ and $E \subset T$ and $T \subset U$

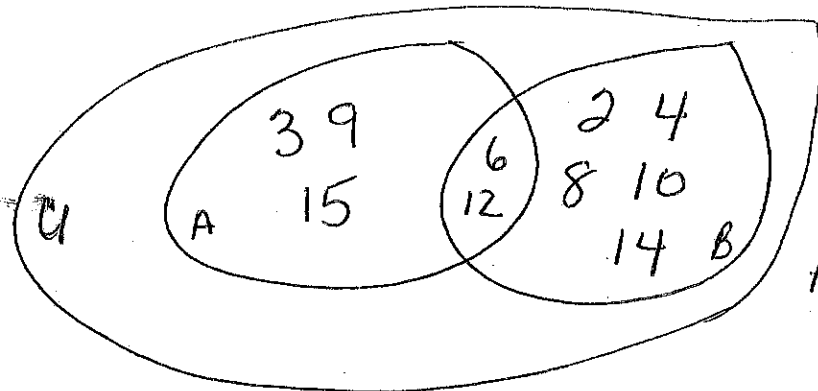
3.2



ex $U = \{2, 3, 4, 6, 8, 9, 10, 12, 14, 15\}$

$A = \{3, 6, 9, 12, 15\}$

$B = \{2, 4, 6, 8, 10, 12, 14\}$



To Draw
find numbers
in common
1st!

$A \cap B = (6, 12)$

- i) in set A = 3, 6, 9, 12, 15
- ii) in set A but not in B = 3, 9, 15
- iii) in set B = 2, 4, 6, 8, 10, 12, 14
- iv) in set B but not in A = 2, 4, 8, 10, 14
- v) in set A and set B = 6, 12
- vi) in set A or set B = 2, 3, 4, 6, 8, 9, 12, 14, 15
- vii) in A' = 2, 8, 4, 10, 14

3.3 Intersection & Union

(A) Intersection = elements in common

ex. $A = \{1, 2, 3\}$ $B = \{2, 3, 4\}$

$A \cap B = \{2, 3\}$

(U) Union = set of ^{all} elements in 2 or more sets

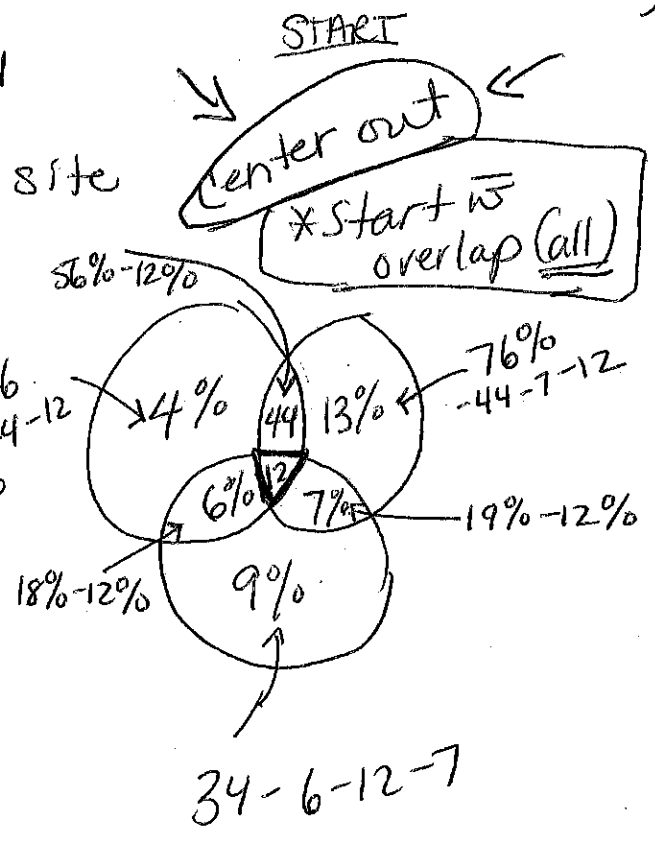
ex. A & B above

$A \cup B = \{1, 2, 3, 4\}$

3.4 Application (How students talk to friends)

C = cell phone - called
 T = texted
 S = social networking site

- 66% cell phone
- 76% texted
- 34% social network
- 56% cell & text
- 19% text & social network
- 18% cell & social network
- 12% all three



Internet search:

You want to find out information about an actor but you can't remember his name.

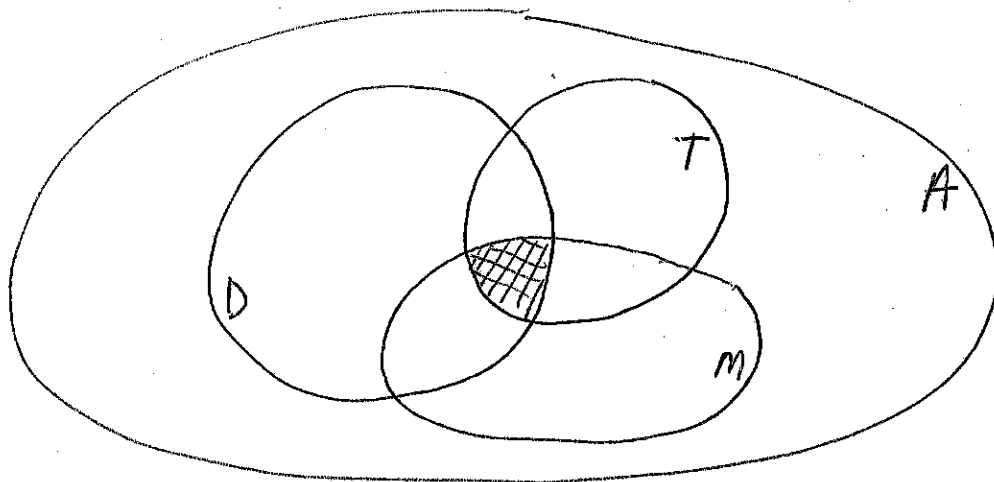
Start \rightarrow actor(A) \Rightarrow way too many results

(D) male, dark hair, young \Rightarrow still too many

(M) drama TV series

(T) 1980's

The diagram would look like this



$D \cap T \cap M = \{ \text{male actor with dark hair, young on a TV drama in the 1980's} \}$

3.5 Conditional Statements + Converse

conditional statement: if-then statement

if _____ \Leftarrow hypothesis
then _____ \Leftarrow conclusion.

Truth table - table of all possibilities

converse - a conditional statement (if-then) where hypothesis + conclusion switch places. (\Leftrightarrow)

Counter example - one that disproves the hypothesis.
 $p \Leftrightarrow q$ means if p then q and if q then p

ex 1 If I swim in the ocean, I am swimming in salt water.

hypothesis - swim in ocean (p)
conclusion - in salt water (q)

Ask - are there any oceans which are not salt water? No \rightarrow so $p \rightarrow q$

Converse: q to p?

Ask swim in salt water does this mean you are in the ocean

* Counter example \Rightarrow Salt water pool.

so q does not lead to p.

ex 2

p = colour blind

q = can't tell difference between colours.

does $p \Rightarrow q$ and $q \Rightarrow p$?

Yes - it can go both ways so $p \Leftrightarrow q$
or biconditional

Truth Table

p	q	$p \Rightarrow q$
T	T	T
F	F	F T
F		

3.6 Inverse + Contrapositive

Inverse \rightarrow if not, then not
(reverse of hypothesis + conclusion)

Contrapositive \rightarrow converse then inverse
 \rightarrow switch hypothesis + conclusion then not them.

ex inverse ~~if~~ if you live in Nanaimo, ^{then} you live in BC
 \rightarrow if you don't live in Nanaimo, then you don't live in BC

*this inverse is untrue.

Contrapositive

\rightarrow if you don't live in BC, then you don't live in Nanaimo.

this contrapositive is true

ex 2 using equations

If a number is a multiple of 10, then it is a multiple of 5.

$$n = \text{a number (a multiple of 10)} \\ = 10x$$

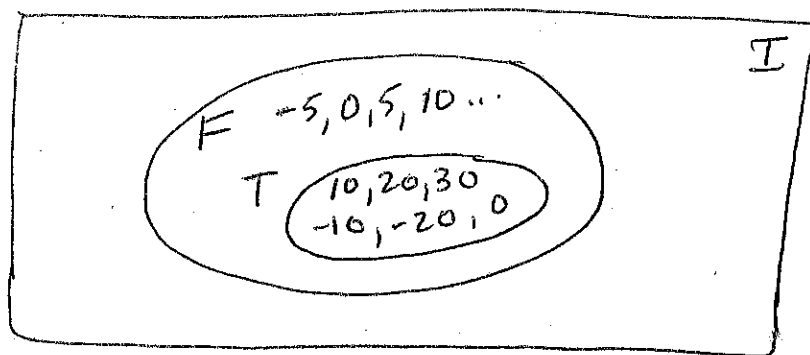
if $n = 10x \Rightarrow$ then $n = 5(2x)$
so a multiple of 5

Contra positive. statement :

If a number is not a multiple of 5, then it is not a multiple of 10

* Since 10 has a factor of 5, then this is true too

ex 12 is not a multiple of 5 so also not a multiple of 10



$$I = \{\text{all integers}\}$$

$$F = \{\text{mult. of 5}\}$$

$$T = \{\text{mult. of 10}\}$$

\therefore to be a multiple of 10 - it must be a multiple of 5.